

$$1. F = x^2 i + (3x+2)j + \sin x k$$

$$a) \frac{dF}{dx} = 2xi + 3j + \cos x k$$

$$b) \frac{d^2 F}{dx^2} = 2i - \sin x k$$

$$c. \left| \frac{dF}{dx} \right| = \sqrt{2^2 + 3^2 + 1^2} \quad \text{i.e. at } x = \left| \frac{dF}{dx} \right| = 2i + 3j + k$$

$$= \sqrt{13}$$

$$d. F \cdot F = [x^2 i + (3x+2)j + \sin x k] \cdot [x^2 i + (3x+2)j + \sin x k]$$

$$F \cdot F = x^4 + (3x+2)^2 + \sin^2 x \quad [i \cdot i = j \cdot j = k \cdot k = 1]$$

$$\frac{d(F \cdot F)}{dx} = 4x^3 + 2(3)(3x+2) + 2 \cos x$$

$$\text{at } x=1$$

$$= 4 + 4(3) + 2(1) = 36 //$$

$$2. r = (t^2 + 3t)i - 2\sin 3tj + 3e^{3t}k$$

$$a. \frac{dr}{dt} = (2t+3)i - 6\cos 3tj + 9e^{3t}k$$

$$b. \frac{d^2 r}{dt^2} = 2j + 18\sin 3tj + 27e^{3t}k$$

$$c. \text{at } t=0;$$

$$= 2i + 0 + 27k$$

$$\left| \frac{d^2 r}{dt^2} \right| = \sqrt{2 + 27^2}$$

$$= 27.07 //$$